Entanglement distribution quantum networking within deployed telecommunications fibre-optic infrastructure

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ABSTRACT

Quantum networks have been shown to connect users with full-mesh topologies without trusted nodes.^{1,2} We present advancements on our scalable polarisation entanglement-based quantum network testbed, which has the ability to perform protocols beyond simple quantum key distribution.^{3,4} Our approach utilises wavelength multiplexing, which is ideal for quantum networks across local metropolitan areas due to the ease of connecting additional users to the network without increasing the resource requirements per user. We show a 10 user fully connected quantum network with metropolitan scale deployed fibre links, demonstrating polarisation stability and the ability to generate secret keys over a period of 10.8 days with a network wide average-effective secret key rate of 3.38 bps.

Keywords: Quantum Communication, Quantum Network, Quantum Key Distribution, Entanglement

1. INTRODUCTION

In the future landscape of Quantum Technology a method of interconnecting different quantum systems will be required. The prevailing direction is towards a Quantum Internet (QI),⁵ constructed by interconnecting Quantum Networks (QNs). QNs have been demonstrated in both metropolitan scale^{6,7} and long distance configurations,^{8,9} however most have focused solely on Quantum Key Distribution (QKD) based networks. This has been the case as the most near term application of a QI is QKD. Methods for building QNs beyond simple QKD have been explored and in general are based on Entanglement Distribution (ED). Such QNs have mainly used photon pair sources to distribute entanglement on a metropolitan scale¹ and across long distance.¹⁰ Some have used single photons from local quantum systems to entangle multiple systems over distance.¹¹ Progress has been made in generating multi-partite entangled photon states,¹² but there are still challenges in producing a scalable network while connect many users together.

As Quantum Technology advances a scalable method of distributing entanglement, that allows for multiple simultaneous use cases, is required. Developing ED QNs for a metropolitan scale area with minimised resource overheads is essential, while still allowing for a system to be scaled up to a larger set of users. The QN discussed below is a based on ED and allows for protocols beyond simple QKD.^{3,4}

2. THE QUANTUM NETWORK

The Entanglement Source (ES) of the QN, shown in Figure 1 (a), is a Sangac Interferometer that produces entangled photon pairs through type-0 Spontaneous Parametric Down Conversion. A continuous wave 775.06 nm laser is used to produce spectrally non-degenerate (different colour) photon pairs with a central wavelength

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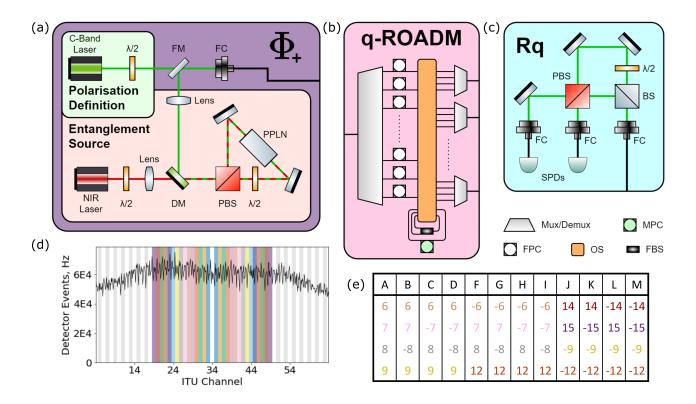


Figure 1. (a-c) show the main components of the Quantum Network. (a) is comprised of the Entanglement Source which produces the entangled photon pairs and the Polarisation Definition which allows for the definition of polarisation bases to be shared amoungst users. (b) is the quantum-enabled Reconfigurable Optical Add-Drop Multiplexer that separates the source signal into 100 GHz ITU channels, routes them, and combines them into a single fibre per user. This systems includes 1-to-4 beam splitters on all demultiplexed channels where $|LC| \ge 6$. Here FPC is a fibre polarisation controller, MPC is a motorised fibre polarisation controller, OS is an optical switch, FBS is a fibre beams splitter, and a (De)Mux is a wavelength (de)multiplexer. (c) is the Quantum Receiver that allow users to measure the single photon signal. Here $\lambda/2$ is a half-wave plate, DM is a dichroic mirror, BS is a beam-splitter, PBS is a polarising beam-splitter, PPLN is a magnesium doped periodically poled lithium niobate crystal, FM is a motorised flip mirror, FC is a fibre collimater, and SPD is a single-photon detector. (d) is the spectrum of the Entanglement Source, where the used International Telecommunication Union channels are shown by bars. Matching channel colour shows entanglement between channels. (e) shows the assignments of Logical Channel to users, where channel colour matches (d).

of 1550.12 nm. Figure 1 (d) shows the frequency spectrum of the ES output, and how that light is cut into International Telecommunication Union (ITU) channels by the quantum-enabled Reconfigurable Optical Add-Drop Multiplexer (q-ROADM), as shown in Figure 1 (b). The central frequency of the output is at 193.4 THz, corresponding to ITU channel 34, such that the entanglement is shared pairwise around this channel. We label ITU channels 19 to 49 as Logical Channel (LC) -15 to +15 respectively.

LCs then share entanglement with their negative counterpart. It is key to note here that all ITU channels, in the range ITU 19-28 and ITU 40-49, have 1-to-4 beam splitters applied to them inside the q-ROADM, such that receiving one LC allows a user to communicate with up to 4 other users. This allows a users to receive one LC in this configuration, where 4 would be required in a configuration without splitting. Although this increases the loss on the links by 6 dB, it reduces the resource requirement of the ES and the q-ROADM by requiring fewer ITU channels to connect all users.

Once separated, each split LC travels though a separate Fibre Polarisation Controller (FPC), and finally each set of LCs are combined into a single fibre. A set of LCs are selected for a single user to receive, such that they share entanglement with all other users in the network, as shown in Figure 1 (e). This may be performed

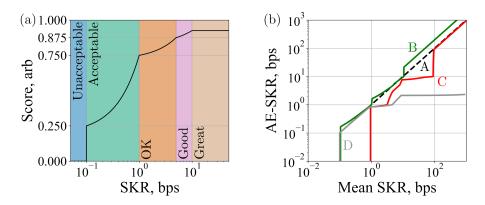


Figure 2. (a) shows the metric through which links in a network are scored according to the Secret Key Rate (SKR). There are 5 main sections. The 'Unacceptable' region, in blue, is where SKR < 0.1 bps, where the SKR is deemed too low so the link is given the fail condition of f(SKR) = 0. The region of 'Acceptable' SKR is where $0.1 \text{ bps} \leq \text{SKR} \leq 1 \text{ bps}$, and is shown in green. The score in this region is linear where $0.25 \leq f \leq 0.75$. A link that is labelled as 'OK', in orange, has $1 \text{ bps} \leq \text{SKR} \leq 5 \text{ bps}$ and has linear score of $0.75 \leq f(\text{SKR}) \leq 0.875$. The 'Good' region, in pink, is where $5 \text{ bps} \leq \text{SKR} \leq 10 \text{ bps}$, and has linear score of $0.875 \leq f(\text{SKR}) \leq 0.925$. A 'Great' link, shown in brown, has $10 \text{ bps} \leq \text{SKR} \leq 10^{12} \text{ bps}$, and has linear score of $0.925 \leq f(\text{SKR}) \leq 1.4 \text{ SKR}$ of above 10^{12} bps is set to f(SKR) = 1, as no increase in SKR will have a real impact on communication speed in a QKD network. (b) shows the relation between the mean of a set of 16 links to the Average Effective Secret Key Rate (AE-SKR). Each show 16 communication links, where **A** has equal SKR in each link, **B** shows where 14 have equal SKR and the remaining 2 have SKR ten time higher than the rest, **C** shows where 14 have equal SKR and the remaining 2 have SKR ten time higher than the rest, links have the same SKR and the final 2 links have a fixed SKR of 0.1 bps.

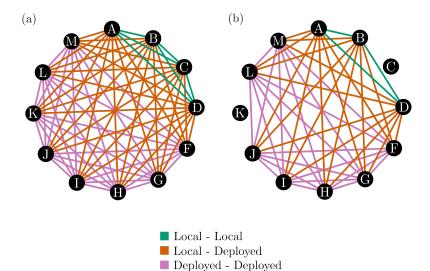


Figure 3. (a) shows the entanglement connectivity of a 12 user full mesh QN. (b) shows the entanglement connectivity of the 10 user fully connected QN discussed. These display the different combinations of local and deployed connections by colour.

dynamically such that the connectivity of a network may be continuously changed. Dynamicity allows for situations where an actively switched network would improve the performance aswell as LC reassignment when network users are changed. The light from the single fibre is then measured by a user inside of a Quantum Receiver (Rq). This measurement has a passive basis choice, preformed by a beam splitter, and then overlaps one of the two measurements from each basis onto one from the other basis reducing the number of Single-Photon Detector (SPD) required at each user. Once all users are receiving photons from the ES, correlations are calculated between every pair in the network, allowing users to generate a Secret Key (SK) through the Bennett-Brassard-Mermin QKD protocol,^{13,14} commonly known as the BBM92 protocol.

This infrastructure constructs a QN consisting of 12 users with a full mesh topology, as shown in Figure 3 (a). There are four remote users; Alice, Bob, Chloe, and Dave each connected through a deployed fibre link with bounce-back link losses of; 1.45 dB, 1,8 dB, 2.74 dB, and 3.24 dB respectively. The remaining eight users; Faye, Gopi, Heidi, Ivan, Jo, Kevin, Lea, and Marek are connected through local fibre.

To assess the quality of the network a metric is required. The mean SKRs of a network often ignore links that are non-functional due to the increased SKRs of other links. We select an interpolation function, as shown in figure 2 (a). This allows the choice of a failure condition in the network, here a link with SKR < 0.1 bps, the score would be 0. A network score is then given by;

$$W = \sqrt[n]{\prod_{i=1}^{n} f(r_i)},\tag{1}$$

where n is the number of links in the QN, r_i is the SKR of link *i*, and *f* is the interpolation function. To retrieve an analogue to the QN mean SKR, taking the score weighing into account, the inverse of *f* can be applied to *W*. This weighted mean is called the Average Effective Secret Key Rate (AE-SKR). The same process can be followed to generate the AE-SKR of a subgroup of links, such as the connectivity scenario or for a single user. Figure 2 (b) shows how a small number of under-preforming link affects the scaling of a network AE-SKR.

3. RESULTS AND DISCUSSION

In order to show entanglement, and therefore generate a SK, between separated users with a shared ES, the definitions of polarisation must match between Rqs. To do this a canonical method of manual fibre neutralisation is used.¹⁵ This is performed by sending an attenuated classical signal comprised of two orthogonal polarisation definitions, Horizontal (H) and Anti-Diagonal (A) light, to the Rqs from the Polarisation Definition setup, as shown in Figure 1 (a). The average polarisation visibility of each user is provided in Table 1. It is clear that 11 of the users have visibilities above 98.7%, however Kevin failed the neutralisation steps with an estimated visibility of ~ 97%. Due to the poor quality of the polarisation visibility, Kevin will not be included in the QN. However, it is key to note here that the estimated Quantum Bit Error Rate (QBER) of the Kevin Links were below 0.1, despite the measurement basis orthogonality issue with the Rq. The timing jitter of the SPDs used by Chloe were significantly higher than other users. As such Chloe is deemed to be a failed user and shall not be included in the QBER being close to the maximum SK generating QBER, but the SKR quickly dropped below the failure condition due to polarisation drifts. The presented QN is therefore a fully

User	Average Visibility		
Alice	0.99505		
Bob	0.99555		
Chloe	0.99213		
Dave	0.98747		
Faye	0.99407		
Gopi	0.99552		
Heidi	0.99533		
Ivan	0.99385		
Jo	0.99715		
Kevin	Failed		
Lea	0.99347		
Marek	0.99564		

Table 1. The average polarisation visibility of Logical Channels being received by each user as measured from the Polarisation Definition.

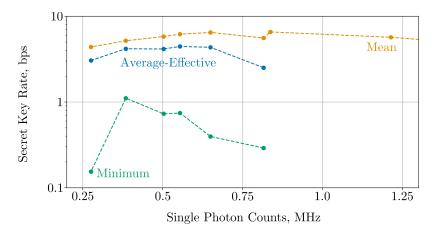


Figure 4. A sweep across the reference single photon rate of the system and the Secret Key Rate (SKR) of the system. The Mean SKR shows the average SKR across the Quantum Network (QN) for the specified singles rate. The Minimum SKR shows the minimum SKR seen across the QN for the specified singles rate. The Average-Effective SKR is calculated from the average score of each link, as shown in Figure 2 (a) and given in Equation 1. From this a singles rate of ~ 0.45 MHz was selected for the QN.

connected 10 user QNs, as shown in Figure 3(b), with no difference in resource allocation to a fully connected 12 user QN, as shown in Figure 3(a).

Once all users are receiving entangled pairs and the definitions of polarisation match, the optimal pump power must be found. This is done by adjusting the laser power and measuring the number of single photon counts measured in an unused LC. Here the reference count rate is measured on LC +3. Figure 4 shows the relation between the reference counts and the SKR. Here it can be seen that the mean SKR remains high for much higher count rates, even past where the minimum SKR is zero. The AE-SKR is consistent between 0.38 MHz and 0.65 MHz, so a corrected count rate of 0.45 MHz was selected for the network.

When the Neutralisation of all QN links is complete network up-time is defined to have started. The count rate of the LCs are set between 1.5 and 2.5 days, as shown by the blue region in Figure 5 (a). Two data points, closest to the selected pump power, are shown in this region. Most users AE-SKR stays stable across the whole time range. Some users; Faye, Heidi, and Jo, fluctuate in AE-SKR after setup but stabilise after some time. One user, Dave, fluctuates across the whole time set and then the link with user Jo fails after 10.8 days of network up-time. This point is the Network Failure point, shown in Figure 5 as as the vertical black line, and the network would be reset. Notably, even though the network was deemed to have failed, the failure was reached by one link dropping to 0.096 bps. As can be seen in Figure 5 (c), the network recovers functionality after the failure condition was reached.

Figure 5 (b) shows the three connectivity scenarios presented in Figure 3 (b). The scenario with the highest AE-SKR was when both users are connected though deployed fibre, with 5.04 bps, as shown in Table 2. This occurred as the detectors with the highest efficiency and Rqs with the lowest loss were given to the deployed users, therefore higher transmission loss is balanced with the more efficient measurement. The scenario where the AE-SKR was lowest was when both users were connected with local fibre. The stability of all three scenarios is similar with approximately 50% fluctuation from the full time AE-SKR to the minimum and maximum AE-SKR. This demonstrates that across the whole 10.8 days there was a stable and fully functional 10 user fully connected QN.

4. CONCLUSION

Here we have demonstrated the setup and operation of a polarisation based 10 user fully connected ED QN, with the resources for a 12 user fully connected ED QN. The QN demonstrated a minimum polarisation stability

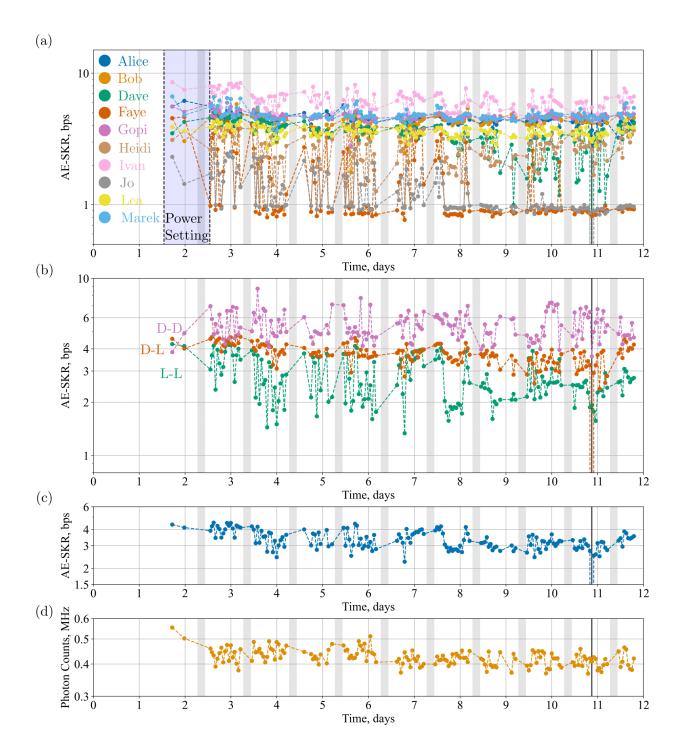


Figure 5. (a) shows the Average Effective Secret Key Rate (AE-SKR) for each user in the network. The blue box represents the time period in which the power per Logical Channel (LC) was set. (b) shows the AE-SKR each connectivity scenario. Here D-D indicates that both users are connected through deployed fibre, D-L indicates that one user is connected through deployed fibre, and L-L indicates that both users are connected through local fibre, and L-L indicates that both users are connected through local fibre. (c) shows the AE-SKR for the 10 user fully connected network, as shown in Figure 3 (b). (d) shows the count rate of the reference LC corrected for loss. All data points in this figure is an average over 10 minutes, and grey boxes indicate when the Single-Photon Detectors stop functioning to cycle the cryogenic gasses.

Scenario	AE-SKR	Maximum	Minimum
Alice	4.4983	6.1654	3.2324
Bob	4.2148	5.8158	1.7643
Dave	3.4391	4.9570	0.9971
Faye	0.9578	4.6524	0.7678
Gopi	4.6861	5.9627	2.7813
Heidi	2.7457	4.0443	0.9795
Ivan	6.1746	8.5474	4.2368
Jo	0.9874	2.6596	0.8514
Lea	3.6083	4.4097	2.6903
Marek	4.7446	6.6571	3.6015
Local-Local	2.7706	4.3851	1.3378
Local-Deployed	3.7769	4.8376	2.5522
Deployed-Deployed	5.0436	8.7522	3.8343
Full Network	3.3818	4.5224	2.2564

Table 2. The Average Effective Secret Key Rate (AE-SKR) of each user, in bps, of each scenario given in Figure 5, before the network failed at 10.8 days. The maximum and minimum are the maximum AE-SKR and minimum AE-SKR respectively, before the network failed.

duration of 10.8 days through both local and deployed fibre links with network wide AE-SKR of 3.3818 bps, as shown in Table 2. Previously, ED QNs based on entangled photon pairs with passive polarisation compensation, with deployed fibre links have only shown up to a day of continuous polarisation stability before the QN is reset.¹ It is also shown that the links between users with deployed fibres demonstrate similar stability to users with only local fibre links. This improvement in stability indicates that the limitation of metropolitan scale ED QNs is likely to be the polarisation stability of the distribution devices rather than the deployed fibre links. The large concentration of fibre lengths that sit in a relatively small area within the distribution devices leads to large polarisation drifts from small environment drifts. Metropolitan scale deployed fibres do not have a large influence on the stability of a QN, and as such scaling QNs up to arbitrary deployed links should be possible, to the limit of the fibre loss of each link.

ACKNOWLEDGMENTS

This work was supported by the UK Engineering and Physical Sciences Research Council (EPSRC) grants EP/SO23607/1, for the Quantum Engineering Centre for Doctoral Training, Centre for Nanoscience & Quantum Information, University of Bristol, and EP/T001011/1 for the Quantum Communications Hub. This work was supported by the Ministry of Science and Education (MSE) of Croatia [contract No. KK.01.1.1.01.0001]

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